ZERODEE

A computer code for 0-D stability analysis

Version 1.4

by CryoSoft

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Introduction

ZERODEE is a computer program for the (parametric) analysis of the stability margin of conductors. It is based on a local balance of heat capacities, i.e. a 0-D model of the cable. The typical conductor, with the geometry indicated in Fig. 1, is approximated lumping each component (helium, cable and jacket) into a single degree-of-freedom. Note that although in principle the helium cross section is subdivided in a portion in the cable bundle and a portion within the cooling hole, the temperature of both portions is considered to be the same (and the helium cross section lumped into a single value).

The set of equations solved by the program is then:

$$
A_{St}C_{St}\frac{dT_{St}}{dt} = \mathbf{F}_{St} + \mathbf{F}_{Joule} - p_{St,He}h_{St,He}(T_{St} - T_{He}) - p_{St,Ja}h_{St,Ja}(T_{St} - T_{Ja})
$$
(1)

$$
A_{Ja}C_{Ja}\frac{dT_{Ja}}{dt} = -p_{Ja,He}h_{Ja,He}(T_{Ja} - T_{He}) - p_{St,Ja}h_{St,Ja}(T_{Ja} - T_{St})
$$
\n(2)

$$
A_{He}C_{He}\frac{dT_{He}}{dt} = \mathcal{F}_{Ja} + p_{St,He}h_{St,He}(T_{St} - T_{He}) + p_{Ja,He}h_{Ja,He}(T_{Ja} - T_{He})
$$
\n(3)

where the subscripts refer to the strands (St), jacket (Ja) or helium (He) in the conductor. The three components, with cross section *A*, have heat capacities *C* that are computed for each cable component as the sum of stabilizer and superconductor (strands), steel and insulation (jacket), and the full helium cross section. A flag allows to compute the helium heat capacity either under constant pressure conditions, or under constant density conditions, thus simulating two extreme processes in a stability transient.

The components are thermally coupled through convection on wetted surfaces (or contact perimeters) *p* with a surface heat transfer coefficient *h*. For the definition of the heat transfer coefficient, the following expressions have been used:

$$
h_{St,He} = h_{He}
$$

$$
h_{Ja,He} = \frac{h_{Ja}h_{He}}{h_{Ja} + h_{He}}
$$

$$
h_{St,Ja} = \frac{h_{Ja}h_{Co}}{h_{Ja} + h_{Co}}
$$

where the following definition has been used for the heat transfer coefficient to helium:

$$
h_{He} = \max\left\{h_{Ks}, h_{Kt}\right\}
$$

\n
$$
h_{Kt} = \frac{h_K h_t}{h_K + h_t}
$$

\n
$$
h_{Ks} = \frac{h_K h_{ss}}{h_K + h_{ss}}
$$

\n
$$
h_K = 200(T_{St} + T_{He})(T_{St}^2 + T_{He}^2)
$$

\n
$$
h_t = \sqrt{\frac{K\rho C_p}{\pi t}}
$$

where *K* is the thermal conductivity of helium, ρ is its density, and C_p is the specific heat at constant pressure and *hss* is the user's defined steady state heat transfer coefficient. For the thermal contacts of strands and jacket the following empirical definitions have been used:

$$
h_{Ja} = \frac{2K_{SS}}{t_{SS}}
$$

$$
h_{Co} = 1000
$$

where K_{SS} is the thermal conductivity of stainless steel and t_{SS} is the thickness of the jacket.

During an evolution, an initial energy input in the strands \oint_{S_t} or in the jacket \oint_{S_a} causes the cable to transit to the normal state. The system of equations above is solved by an implicit, linearised, first order accurate algorithm that is unconditionally stable. Adaptive time stepping, based on a limit on the maximum change in the solution, is used. The user can select the minimum and maximum allowed time steps to be taken, thus allowing for a limited control on the actual time stepping.

The evolution of the system is followed until quench or recovery can be decided. Time limit, as set by the user, is signalled by an error condition when reached. The decision on recovery or quench is based on the following algorithm:

- recovery if $t > \tau_q$ and $V \leq V_{max}$
- quench if ($t > \tau_q$ and $T_i > T_c$) or ($t > 1.5 \tau_q$ and ($V > V_{max}$ or $\frac{dV}{dt} > 0$))

where τ_q is the heating time (in s), *V* is the resistive voltage (in V/m) and $\frac{dV}{dt}$ is its time derivative,

 V_{max} is the user's selected voltage threshold for quench detection (in V/m), T_c is the critical temperature (in K)*.*

An external loop keeping track of the energy input in the system is adjusting automatically searching for the energy margin between an upper and a lower bound determined by the user. Again, an error condition signals the fact that the energy boundaries are too tight (and the actual energy margin is below or above the bracket).

As a final feature, the program loops on the input file to search for new cases. The input data needs to be modified only for what concerns the changing parameters, all other data are maintained equal to those read for the previous case. A storage file stocks the results of the cases, and a postprocessor, reading the results stored, allows the creation of tables for plotting of the energy margin versus a parameter (within the definition of allowed parameters in the post-processor).

The input of the processor has been thought for maximum compatibility with the 1-D analysis code *GANDALF*, so that *ZERODEE* can be effectively used as a preliminary tool for a more sophisticated analysis.

Figure 1. General geometry of a conductor considered in *ZERODEE*.

Code Structure

Main solver

This is the portion performing the calculation and generating the results. The code performs input and output on the following files

The binary storage is used for post-processing by the program *ZERODEEP* (see later for its description).

Note: FORTRAN unit numbers above 50 are reserved for internal use

Material properties

The main solver needs to be linked to a set of routines for the calculation of the material properties of solid materials and helium. As these routines are at the lowest level in the code execution, their efficiency is of paramount importance. A set of routines is provided by default with the program. These can be easily changed provided that the calling arguments are respected (and obviously units !) and keeping in mind the requirements on the code efficiency. For the complete list of the property functions, please refer to the *SOLIDS* [1] and *He_tables* [2] manuals.

Input Variables

The following table contains the input variables, their physical dimensions, default value and meaning for the *ZERODEE* processor. They have been kept compatible with the input to *GANDALF* as far as possible. The input of *ZERODEE* is done using the FORTRAN instruction NAMELIST. The namelist is called INDATA. A sample input file is reported in the end of the manual. Note that the first line in the input file is read-in as the problem title.

WARNING ! Note that the *ZERODEE* model needs a positive heat capacity for all three cable components. This implies that the following constraint must be satisfied :

Variable	Type	Units	Default	Meaning
IOP ₀	R	(A)	0.0	Initial operating current in the coil
IOPFUN	I	$\left(-\right)$	$\mathbf{0}$	Flag used to specify the behaviour of the operating current in time: user's defined. through external (-1) function EXTI to be linked with the code (0) constant in time
IBIFUN	\bf{I}	$\left(-\right)$	$\mathbf{0}$	Flag used to specify the behaviour of the magnetic field in time and space user's defined, through external (-1) function EXTB to be linked with the code (0) constant in time at the value BISS and BOSS (1) Proportional to the current in time. At any time the field is the sum of the steady state value BISS and of the transient value proportional to the operating current BITR
BISS	R	(T)	0.0	Value of the steady state component of the magnetic field
BITR	R	(T)	0.0	Value of the transient component of the magnetic field

Operating conditions

Time stepping and quench/recovery decision

Variable	Type	Units	Default	Meaning
TIMLIM	R	(s)	0.0	Maximum time for the time integration (time limit)
VMAX	R	(V/m)	0.0	Voltage threshold used to determine the quench or recovery condition during an evolution. The conductor recovers if after the heating time TAUQ the resistive voltage is below the threshold VMAX, while it has quenched if the voltage is above VMAX (see the quench/recovery decision algorithm described in the introduction)
STPMIN	R	(s)	0.0	minimum allowed time step
STPMAX	R	(s)	0.0	maximum allowed time step

The input file consists in general of a title card, followed by an arbitrary number of input data sets (cases). *ZERODEE* loops on the input cases automatically, solving all of them. Note that in the input phase the previous value of the parameters is retained (if not explicitly given in the new case). Therefore the input of new cases with a change in a single parameter is extremely simplified (the namelist for the case contains the single parameter to be changed). See in the example section for a real input case.

External Routines

The following sections describe routines that are provided as an interface for the user to improve the modelling capabilities of *ZERODEE*. These routines are provided as dummy (void) procedures, in the case that they are not needed for the standard execution of the code.

Note: FORTRAN unit numbers above 50 are reserved for internal use

Coil current

Compute the operating current as an arbitrary function of time and coil resistance.

List of variables:

Magnetic field

Compute the magnetic field as an arbitrary function of time and current

External heat input

Compute the heat perturbation as an arbitrary function of time and space. The routine returns the value of the heating flux in the conductor QFLUXC or in the jacket QFLUXJ at the time TIME. Note that the parameter TAUQ read-in from the input namelist (see input parameters list) is passed to the routine (as *trimming* value) although it is in effect not used in the main program (but can be used in principle in EXTQ). The variable E0 is the trial linear energy density (J/m) that must be input in total in the conductor, as determined by the solver in its search for the energy margin. This means that the time dependence of the heat fluxes must be such that their time integral is E0. Finally, in the recovery/quench check, TAUQ is used as the maximum time over which heating takes place. This means that after TAUQ the heating must be off (or negligible) for the check in the solver to be valid.

Electrical and thermal properties of user's defined materials

These functions substitue the default material properties in case of negative material flag ISC.

Density

Used to compute the density of a user's defined material

List of variables:

Specific heat

Used to compute the specific heat of a user's defined material

Critical current density

```
FUNCTION UserCriticalCurrentDensity (Material ,T ,B ,ANGLE ,
                       EPSLON)
```
Used to compute the critical current density of a user's defined superconducting material

List of variables:

Critical temperature

Used to compute the critical temperature of a user's defined superconducting material

List of variables:

Current sharing temperature

Used to compute the current sharing temperature of a user's defined superconducting material

Error Codes

A limited number of checks are performed in the input phase to insure that the data set is consistent and that the memory requirements for the solution of the problem do not exceed the availability. An error message is printed on the main output unit in case that one of these checks is not passed. The error message gives a numeric code which corresponds to the following table:

Post Processing

For post-processing of the results of *ZERODEE*, an easy to use interface has been written: *ZERODEEP*. This program reads the storage file and prompts, through a menu, for a selection of the variable to be considered as the independent parameter. An ASCII table is then created with the case number, the value of the parameter and the computed energy margin (in J/m and in mJ/cc referred to the strand cross section). The list of allowed parameters is shown in Fig. 3, where the menu list is reported. Selection is by numeric input.

 <<< ZERO-DEEP >>> Enter Your Choice: ---------------------------------- Energy Margin as a function of: (1) Superconductor area (2) Stabilizer area (3) Helium area (4) Steady state h (5) Strain (6) Electric field E0 (7) Power law exponent (8) Stabilizer RRR (9) Field (10) Operating current (11) Pulse duration (12) Initial pressure (13) Initial temperature ---------------------------------- (0) END EXECUTION ----------------------------------

References

- [1] CryoSoft, *SOLIDS – Properties of Solid Materials*, Version 3.3, User's Manual, October 1999
- [2] CryoSoft, *He_tables – Helium Properties*, Version 2.1, User's Manual, February 1999

Examples

Here are reported the input data for a sample run performed with the basic version of *ZERODEE* (i.e. without user's adaption, standard material properties) on a parametric analysis with the operating current as a parameter, and the results obtained using the post-processor *ZERODEEP*.

Input for a run with ZERODEE

```
ZERODEE Test Run for the manual
&INDATA
      AHEH = 19.6E-6, AHEB = 71.4E-6,
      ASC = 40.6E-6, AST = 60.8E-6, AJK = 73.5E-6,
     ISC = 4002, RRR = 100.0, AIN = 61.0E-6,PHTC = 0.330, PHTJ = 5.1E-2, PHTCJ = 0.0E+0,
     E0 = 1.0E-4, NPOWER= 20, EPSLON=-0.250E-2,
     \text{IIN} = 22, \text{IST} = 1, \text{IJK} = 13, INTIAL= 1, 
     PREINI= 6.00E+5, TEMINI= 4.5,
     HSS = 0.0, IOPFUN= 0,
     IOPO = 8.00E + 3, IBIFUN= 0,
     BISS = 10.0, BITR = 0.0,
     IQFUN = 0,<br>FOMIN = 5.00.
             5.00, E0MAX = 1000.00,
     TAUQ = 10.0E-3,VMAX = 1.0E-4, STPMIN= 1.0E-5, STPMAX= 1.0E-3,
      TIMLIM= 1.0
&END
&INDATA
     IOPO = 7.00E + 3,&END
&INDATA
     IOPO = 6.00E+3,&END
&INDATA
     IOPO = 5.00E+3,&END
&INDATA
    IOPO = 4.00E + 3,&END
&INDATA
    IOPO = 3.00E+3,&END
&INDATA
    IOPO = 2.00E+3,&END
```
Post processor ZERODEEP

In accordance to the previous input, with operating current as a parameter, the following table was obtained with *ZERODEEP* (file TEST.TABLES) after responding to the menu prompt with the option "10" (Operating current). Note the value of energy margin in J/m converted in mJ/cc of strand (i.e. based on superconductor plus stabilizer cross section)

